

# **FAN CHART:**

## The art and science of communicating uncertainty

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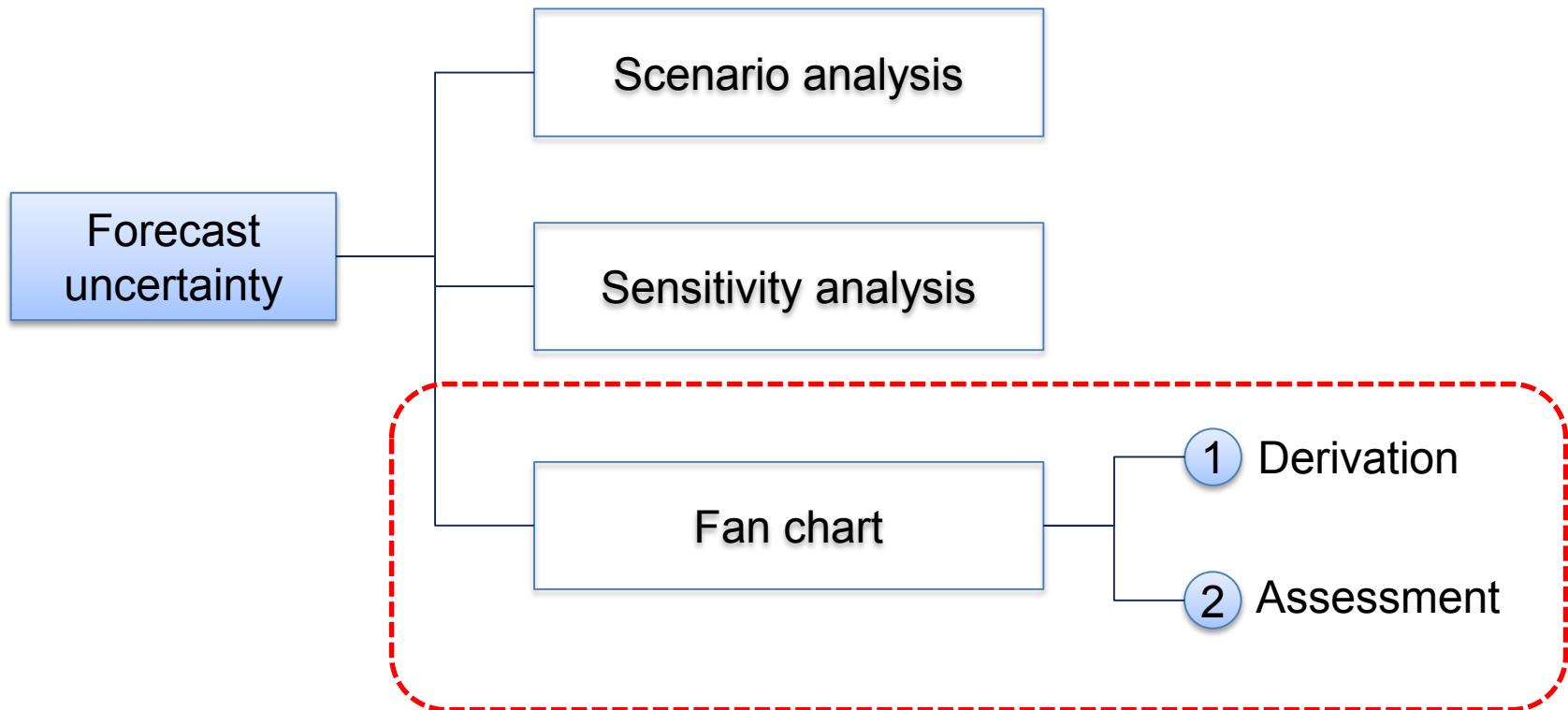
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*\*The views expressed in this presentation and the corresponding paper belong to the authors and do not represent the views of Bank Negara Malaysia*

# Forecast uncertainty can be assessed in three ways



# Constructing the fan chart: Deriving the three key parameters of the fan chart

## Parameters

1 Central projection

## Derivation method

**Baseline forecast** of the variable ie GDP or inflation

2 Uncertainty (Width)

**Historical forecast errors**, adjusted for uncertainty of key assumptions (risks factors) affecting the baseline forecast eg ER, commodity prices, etc.

Historical forecast standard error

$$\sigma_{infl} = \sigma_e \sqrt{\frac{\sum w_i x_i}{\sum w_i \bar{x}_i}}$$

Uncertainty of forecast assumptions (now compared to past)

$w_i$  = elasticity of assumptions  
 $x_i$  = current volatility of assumptions  
 $\bar{x}_i$  = historical volatility of assumptions

3 Balance of risks (Skew)

**Linear combination of the skew of risks factors**, obtained from subject matter experts

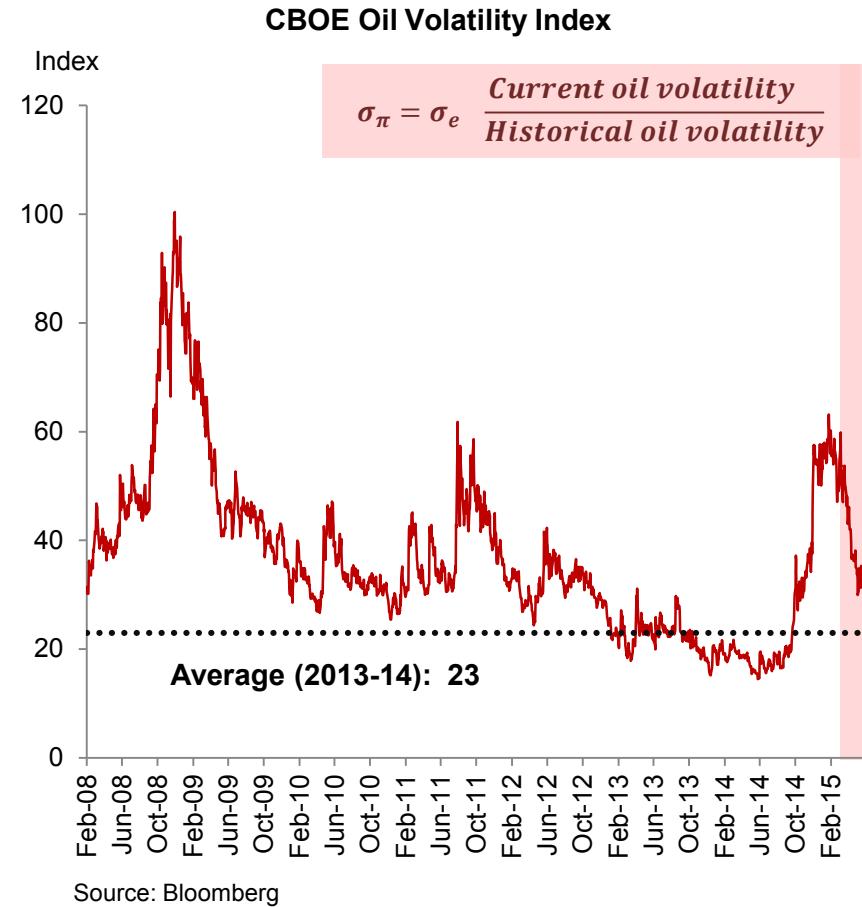
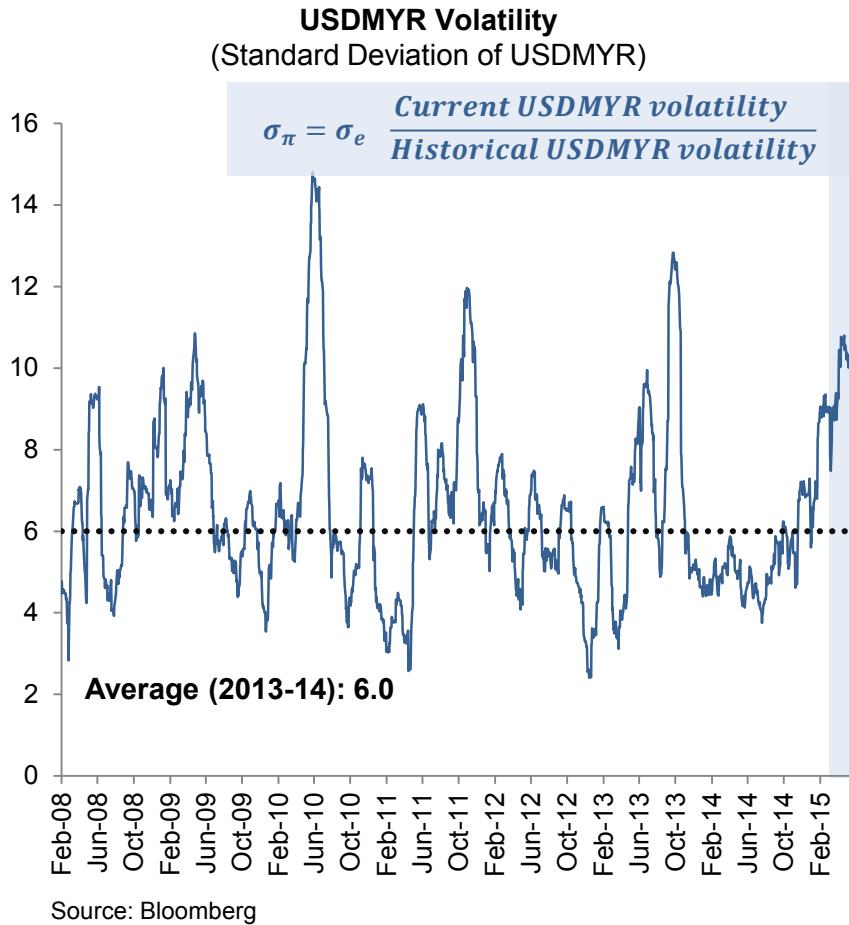
$$\gamma_{infl} = \sum w_i \gamma_i \quad \text{where} \quad \gamma_i = \sqrt{\frac{2}{\pi}} (\sigma_u - \sigma_l)$$

**Assumptions:**

1. Distribution of variable and risks factors are assumed to be TPN
2. Maximum of the analyst forecast represents the upper 90% confidence level and the minimum represent the lower 90%. This is used to compute the upper and lower standard deviation of TPN ( $\sigma_u, \sigma_l$  respectively)

# Width: Forecast uncertainty incorporates the uncertainties of risk factors

- The adjustment to the overall forecast uncertainty is based on the volatility of the assumption relative to the historical value of volatility

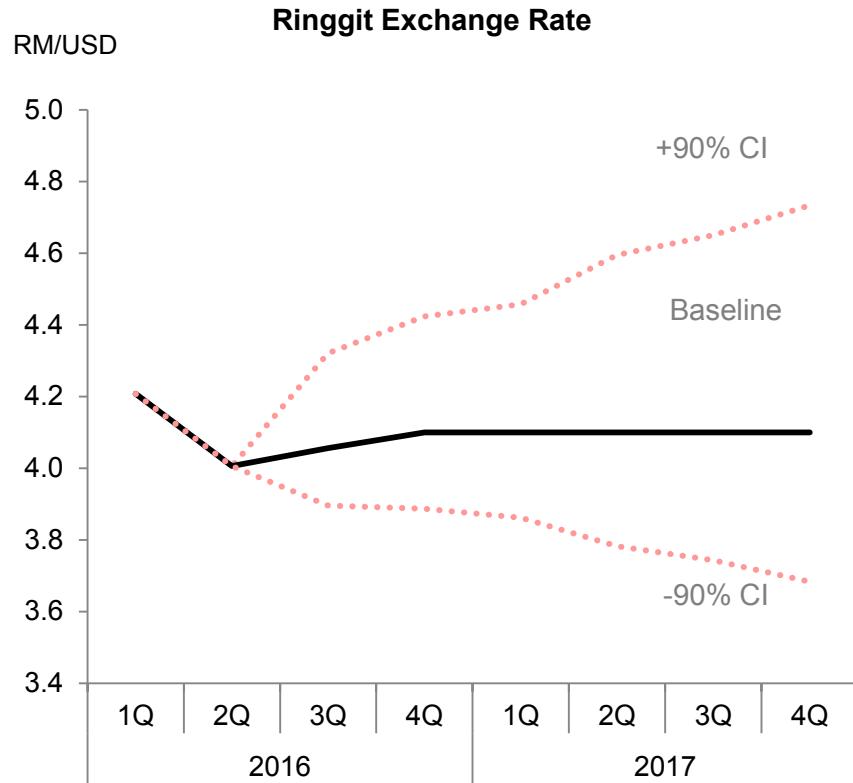


Main

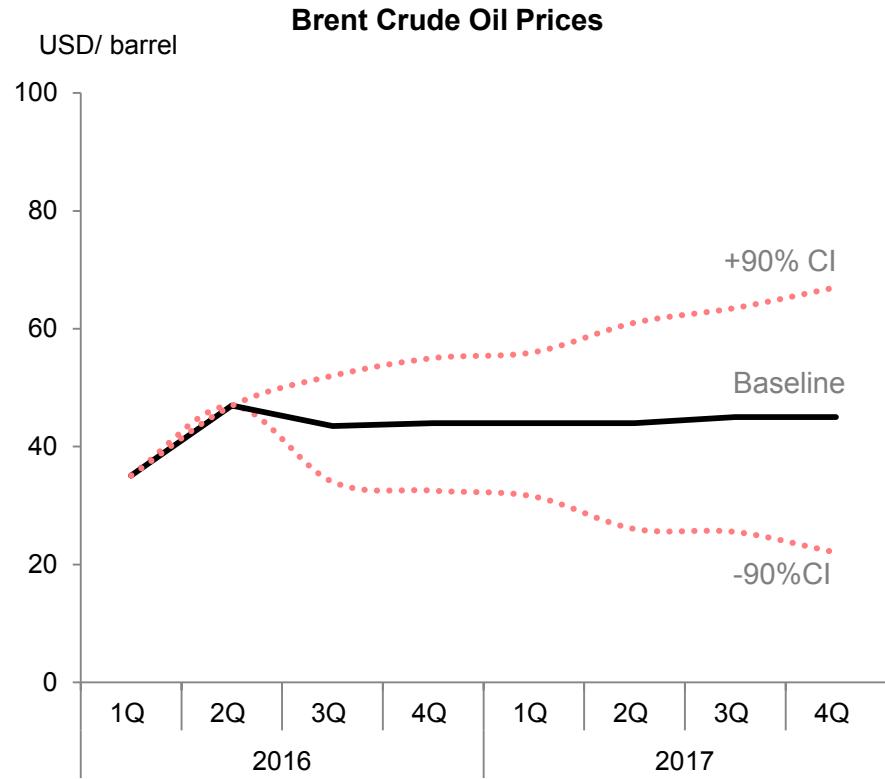
# Skew: Overall balance of risk also incorporates the skew of each risk factors

- Balance of risks of each risk factors are obtained from the respective subject matter specialists

Depreciation risks to the ringgit exchange rate



Downside risks to global oil prices

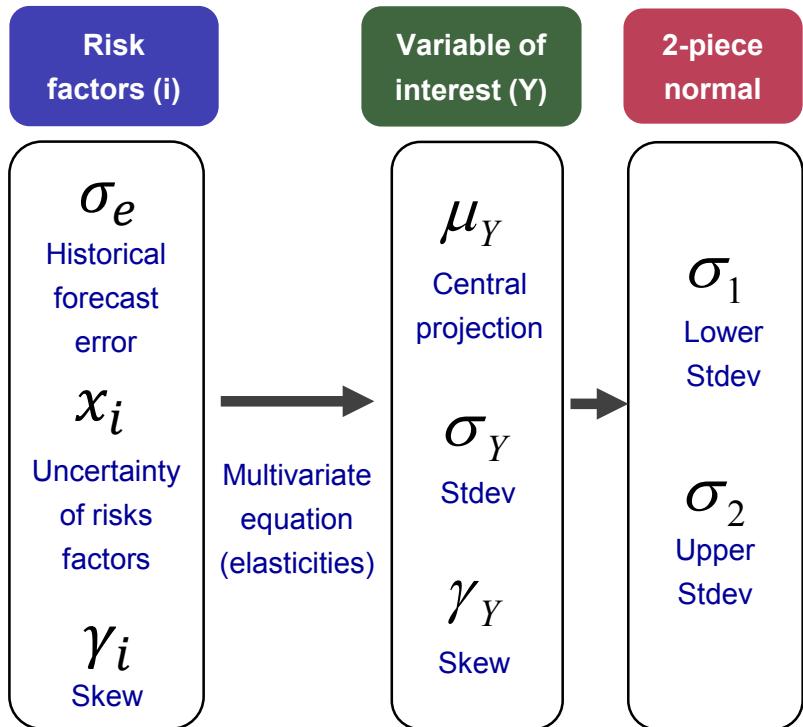


Main

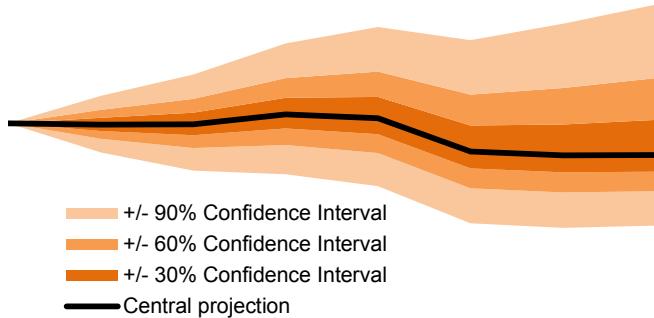
# Information of risk factors are incorporated to compute the probability distribution

To construct the fan chart:

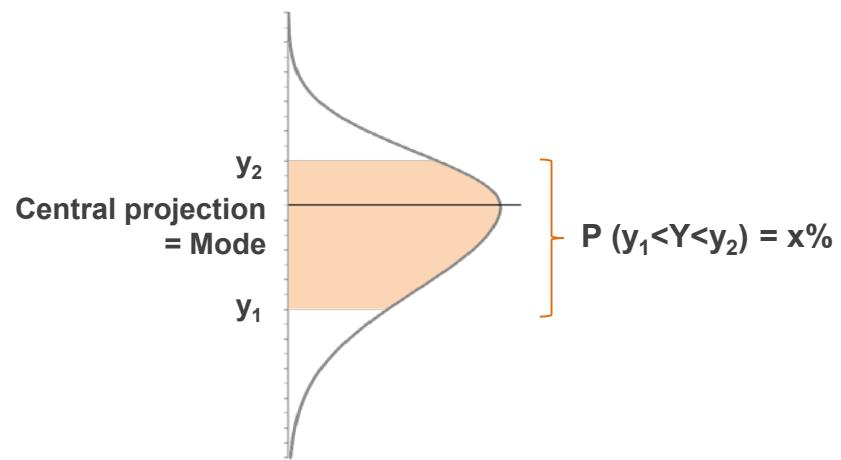
Combine three key parameters  
using the two-piece normal distribution



A. Deriving upper and lower bands of a fan chart

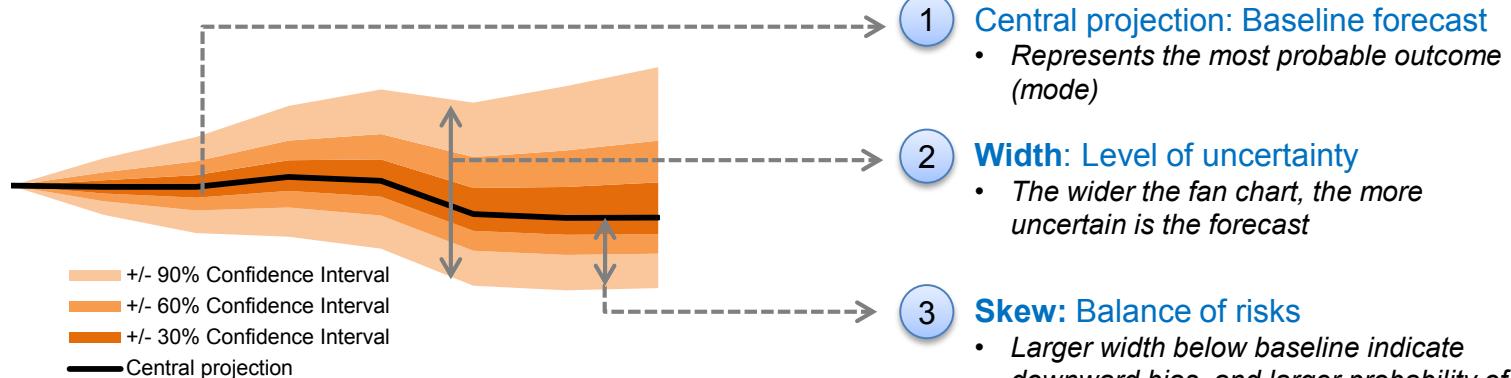


B. Computing probability of a given forecast range

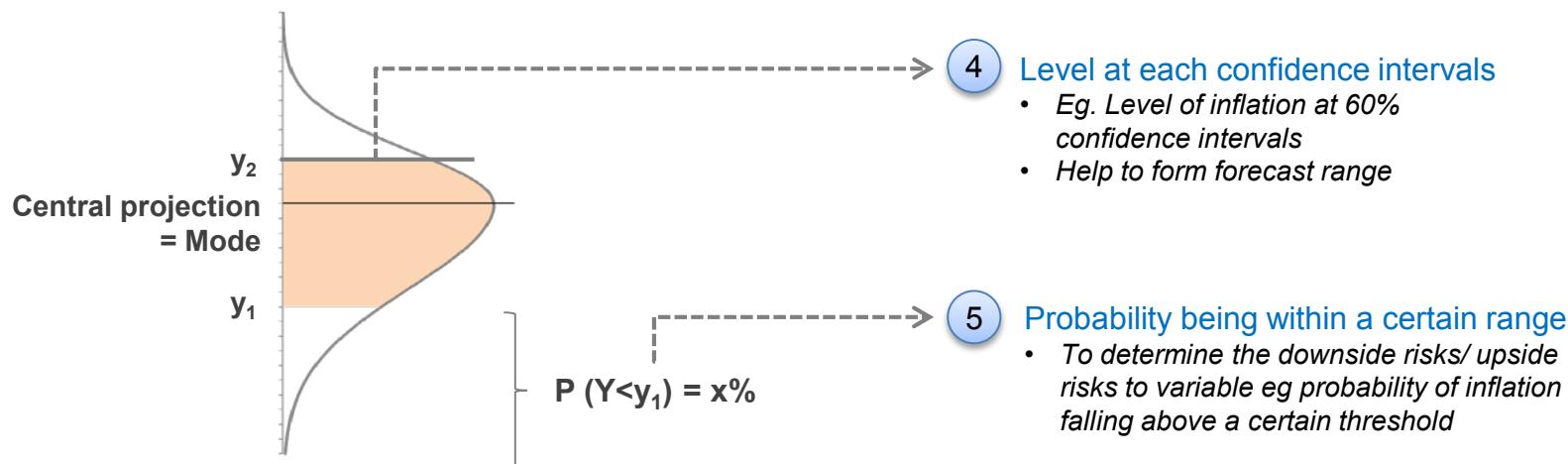


# Fan chart enables probabilistic analysis of risks surrounding the forecasts

## A. Fan chart provides the balance of risks of the forecasts



## B. Splicing the fan chart provides the probability distribution at any point in time



# It contains abundant of information to support policy making

1. *What level of uncertainty surrounding the forecasts?*
2. *Where does the balance of risks lie?*
3. *What contributes to the balance of risks?*
4. *What is the probability of being within(outside) the forecast range?*
5. *How has the balance of risks surrounding the forecast have evolved?*

# Thank you

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